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# Soil-bridge system stiffness identification through field and laboratory measurements

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## Abstract

Despite the major advances in finite element (FE) modeling and system identification (SI) of extended infrastructures, soil compliance and damping at the soil-foundation interface are not often accurately accounted for due to the associated computational demand and the inherent uncertainty in defining the dynamic stiffness. This paper aims to scrutinize the effect of soil conditions in the SI process and to investigate the efficiency of advanced FE modeling in representing the superstructure-soil-foundation stiffness. For this purpose, use is made of the measured, computed and experimentally identified natural frequencies of a real bridge. Field measurements that were obtained during construction were reproduced both in the laboratory and by refined FE modeling. In addition, to understand the physical problem more thoroughly, three alternative soil conditions were examined, namely, rock, stabilized soil and Hostun sand. Discrepancies in the order of 3-13% were observed between the identified and the numerically predicted natural frequencies. These discrepancies highlight the importance of reliable

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estimation of soil properties and compliance with the SI framework for extended bridges under ambient and low amplitude vibrations.

## **Introduction**

It has long been shown through scientific research worldwide that structural engineering projects should not be designed without considering the effect of soil conditions, especially in the case of structures of major significance or those resting on soft and/or varying soil profiles (see Sextos, 2014 for a summary). The most comprehensive way of accounting for soil stiffness is to study the structure-foundation-soil system as a whole (Wolf, 1989). However, due to the high computational demand associated with FE modelling, alternative methods have been developed. These methods involve kinematic and inertial decoupling through the appropriate modeling of dynamic stiffness for different foundation shapes (circular, rectangular, arbitrary), embedment depths (surface, shallow embedded, intermediate embedded, pile) and foundation subsoils (deep uniform deposit, multi-layer deposit, shallow stratum over rock) (Veletsos and Wei, 1971; Dominguez and Roesset, 1978; Wong and Luco, 1985; Kausel, 1974; Gazetas et al., 1985). In particular, shallow embedded circular foundations and caissons (i.e., with a length-to-diameter aspect ratio,  $D/B < 2$ ) are commonly modeled by replacing the foundation-soil system with six degrees of freedom (6 DOF) springs, the stiffness of which is typically calculated according to Elsabee and Morray (1977) and Gazetas et al. (1985). Alternatively, shallow embedded foundations are also treated as intermediate embedded foundations (with a length-to-diameter aspect ratio,  $2 < D/B < 6$ ). Based on this approach, the subsoil may be replaced by 6-DOF springs lumped at the base of the foundation (Kausel, 1974; Kausel & Ushijima, 1979), while additional 6-DOF springs are attached at the middle of the foundation height (Gerolymos and Gazetas, 2006; and improved by Varun et al., 2009). Notwithstanding the major advances made in quantifying the stiffness of the soil-bridge system, the reliable validation of the above spring coefficients remains an open issue with a significant

44 impact for the safety of bridge engineering projects. The majority of experimental work  
45 conducted along these lines consists of laboratory testing of specific foundation-soil  
46 components, tested either on a shaking table or in a centrifuge, as well as entire scaled bridge-  
47 foundation-soil systems without the superstructure (Finn, 2005). Based on the responses  
48 measured in the laboratory, various constitutive laws and numerical predictions of soil stiffness  
49 have been compared, verified and/or optimized.

50 Alternatively, implicit on-site evidence regarding the effect of soil-structure interaction on the  
51 dynamic and seismic responses of bridges has also been provided by means of SI, for example,  
52 on real bridges (Crouse et al., 1987; Chaudhary et al., 2001; Todorovska, 2009;) on a bridge  
53 replica at a test site (Manos et al., 2014) and on buildings (Stewart et al., 1998; Taciroglou et  
54 al., 2014; Shamsabadi et al., 2016). SI is an advanced tool for the inverse prediction of the  
55 dynamic characteristics (i.e. natural frequency, damping ratio and mode shape) of structures that  
56 also accounts for the inherent properties of the supporting soil. The results of SI are usually  
57 exploited to validate the developed finite element models by comparing and ultimately matching  
58 the identified and the numerically predicted dynamic characteristics of a structure. Critical  
59 reviews, qualitative and quantitative comparisons among alternative SI methods based on  
60 benchmark structures, as well as their recent developments are expounded in the literature  
61 (Andersen et al., 1999; Peeters and De Rock, 2001; Peeters and Ventura, 2003; Antonacci et al.,  
62 2012; Reynders, 2012).

63 Based on the above, it is clear that the impact of soil-structure interaction on the dynamic  
64 response of a bridge-foundation-soil system is most commonly validated either in the laboratory,  
65 with controlled soil conditions but subject to the inevitable limitations of scaling, or on-site, that  
66 is, in real scale but without laboratory-controlled soil conditions or the potential to study the  
67 relative effects of different soil stiffnesses. These limitations hinder the appraisal of existing  
68 analytical solutions and numerical approaches for considering soil stiffness under both realistic

scale and soil conditions. Along these lines, the scope of this paper is to study the implications of soil-structure interaction on the modal identification of a real bridge-soil system by making use of measurements obtained at both the macro (prototype) and the laboratory scales, and by utilizing in-situ ambient vibrations and artificially produced ambient loads, respectively. The above comparison enables (a) the validation of different, widely used modeling approaches and spring constants against measured data, and subsequently (b) the comparative assessment of the impact of alternative soil conditions on the extracted modal parameters of the soil-structure interacting system.

The case studied herein is a segment of the (527 m long) Metsovo bridge in Greece. Ambient vibration measurements were obtained at the level of the deck at the construction stage (Panetsos et al., 2010) during which the partially constructed bridge was responding as a T-shaped cantilever. The apparent advantage of this particular case is that at the time of construction the (single, at this stage)  $M_3$  pier-deck segment consisted of a simple and easy-to-model-and-test structural system (Figure 1). In addition, its stiff foundation soil facilitated the construction of a dynamically equivalent system at the laboratory, because the uncertainty associated with the soil conditions was relatively minor (Figure 2). The latter equivalent system had been studied under similar (rock) conditions at the laboratory before its response was extrapolated for the case of alternative soil conditions (i.e., stabilized soil and Hostun sand). The laboratory and the on-site identification campaigns, as well as the development of alternative numerical models and the subsequent quantification of their associated model qualities are presented in the following sections. A synopsis of this work that focuses exclusively on a single type of soil can also be found elsewhere (Faraonis et al., 2014).

## **Prototype structure**

### ***Description of the structural system***

The Metsovo ravine bridge was constructed in 2008 in Greece along the 650 km Egnatia

Highway. The bridge was constructed with the balanced cantilever construction method, which made feasible the modal identification of structurally independent T-shaped cantilever bridge segments during construction. The modal characteristics of pier  $M_3$  and the respective deck segment (Figure 1) were identified by Panetsos et al. (2010) prior to the construction of the key section, which connected the segment to the  $M_2$  pier-deck (that acted as a temporary, balanced cantilever). At the time the measurements were obtained, the total length of the deck temporarily supported by the  $M_3$  cantilever was 215 m, while the height of the pier itself was 32 m. The pier was founded with a large caisson in subsoil characterized by thickly bedded interchanges of sandstones and limestones. More specifically, the subsoil mechanical properties have been defined as follows: i) vertical and horizontal friction angle,  $\phi_v=25^\circ$  and  $\phi_h=35^\circ$  (based on shear strength laboratory tests), ii) vertical and horizontal cohesion,  $c_v=100 \text{ kN/m}^2$  and  $c_h=100 \text{ kN/m}^2$  (also based on the same set of tests), iii) unconfined compression strength,  $q_u=15 \text{ MPa}$  (based on unconfined compressive strength laboratory tests) and iv) one-dimensional confined compression modulus,  $E_{o,static}=1/mv=400\text{-}1000 \text{ MPa}$  (based on Menrad Pressuremeter field tests). Furthermore, Lugeon field tests depicted no evidence of a permanent underwater aquifer in the vicinity of the bridge. Column 1 of Table 1 summarizes the section and material properties of the prototype structure (referred to as “actual structure” hereafter for the purposes of comparison with the laboratory models).

### *System identification of the prototype structure*

The modal identification of the  $M_3$  cantilever was based on ambient vibration measurements triggered by wind and operational loads. Five frequencies were successfully identified, in the range of 0.159-0.908 Hz, as shown in Table 2; column 1 of the table corresponds to one rotational, two longitudinal, one transverse and one bending mode of vibration. Detailed information regarding the measurements, the accelerometer installation configuration and the applied identification methodology can also be found in Panetsos et al. (2010).

119

**Fixed scaled structure****Scaling laws & dimensional analysis**

121 The construction of a scaled structure primarily determines the scaling laws relating the material  
 122 and geometry of the prototype to those of the scaled structure. These scaling laws can be  
 123 determined either by dimensional analysis or the analysis of the system's characteristic equation.  
 124 Based on dimensional analysis and by neglecting the gravity distortion effects that inevitably  
 125 arise during scaling, the scaling factor that relates the natural frequencies of a scaled structure  
 126 with its prototype can be taken as (Bridgman, 1931):

$$\lambda_f = \frac{1}{\lambda_l} \cdot \sqrt{\frac{\lambda_E}{\lambda_\rho}} \quad (1)$$

127 where:  $\lambda_f$  is the prototype to the model frequency ratio,

128  $\lambda_l$  is the prototype to the model dimension ratio,

129  $\lambda_E$  is the prototype to the model Young's modulus of elasticity ratio,

130  $\lambda_\rho$  is the prototype to the model density ratio.

131 Based on Equation 1, it is evident that if the construction of a scaled structure that is identical  
 132 to the prototype was indeed feasible at a 1:100 scale ( $\lambda_l=100$ ) using the same materials is the  
 133 actual structure ( $\lambda_E=1$  and  $\lambda_\rho=1$ ), then the prototype to the model frequency ratio would be equal  
 134 to  $\lambda_f=1/100$ . In such a case, this theoretically scaled model would have the section and material  
 135 properties presented in column 2 of Table 1, and its natural frequencies would vary between  
 136 15.90 and 90.80 Hz, as also shown in the same column. These (ideally, acquired) natural  
 137 frequencies are therefore deemed in this study as the *target* dynamic properties of the fixed  
 138 scaled model constructed in the laboratory.

**Construction of the fixed scaled structure**

140 Given the long deck of the T-shaped prototype cantilever (which was extended to 215 m as seen  
 141 in Figure 1) and the limited space available in the laboratory, the scale of the equivalent structure

was set to 1:100. This particular scale did not enable the construction of an exact replica of the concrete deck section, because this would have resulted in web and flange dimensions as thin as 22 mm and 3 mm, which are impossible to cast. As a result, an equivalent steel structure was designed to represent the same dynamic characteristics as the ideally scaled structure, after appropriate optimization of the dimensions were made to match those of standard sections that were available in the market. The optimization of the equivalent section dimensions was performed numerically using the FEA software ABAQUS 6.12. The model was fixed at its base in order to represent the stiff foundation soil of the actual conditions of the prototype structure. The above procedure resulted in an equivalent steel balanced cantilever, which was assembled using the following commercially available sections (Figure 2):

- a 90×90×3 HSS hollow steel section of 215 cm length corresponding to a 1:100 replication of the prototype deck,
- a 100×100×5 HSS hollow steel section of 6.15 cm length corresponding to a 1:100 replication prototype of the central deck-segment,
- two 80×20×3 HSS hollow steel sections of 32 cm length corresponding to a 1:100 replication of the prototype, twin blade,  $M_3$  pier, and
- a 100×100×5 steel plate, which was used as the base of the pier. Four holes enabled the above steel sections to be bolted and fixed to a laboratory shaking table. These holes were also used later to bolt the pier deck system to the caisson embedded into the soil.

The section and material properties of the fixed scaled structure are summarized in column 3 of Table 1.

### ***Stochastic subspace identification***

To identify the natural frequencies, mode shapes and damping ratios of the fixed scaled structure, an output-only ambient vibration-based SI process was applied involving the covariance-driven stochastic subspace identification method available in the MACEC Matlab



toolbox (Reynders & De Roeck, 2007). More information regarding this method can be found in Van Overschee and De Moor (1996) and Peeters and De Roeck (1999). A hammer was used to excite the structure at the deck level, thus resembling the broadband nature of the actual ambient vibration of the actual structure. It should be noted that this broadband type excitation is consistent with the utilized modal identification method adopted; however, it is not intended to be used for non-stationary excitations (i.e., for seismic assessment purposes).

### *System identification of the fixed scaled structure*

The scaled structure was constructed in the Soil Mechanics laboratory at the Bauhaus University Weimar, in Germany, and was fixed initially on the base of the shaking table. This particular “baby” shaking table has dimensions  $1 \times 1 \text{ m}^2$  and is capable of imposing 35 mm displacements within the frequency range of 2.5-30 Hz. Six triaxial accelerometers placed along the longitudinal, transverse and vertical directions were installed on the structure. Five of those were set up on the deck and one at the base of the pier. Three of the above six sensors, namely RS<sub>1</sub>, RS<sub>2</sub> and RS<sub>3</sub>, were considered as the reference sensors (RS) and thus remained steady. Sensors S<sub>4</sub>-S<sub>6</sub> were placed in three alternative configurations (C1, C2 and C3; Figure 3). All accelerometers were of the same type (Model 356A16 by PCB Piezotronics Inc): weight 7.4 g, frequency range 0.3-6000 Hz and sensitivity 10.2 mV/(m/sec<sup>2</sup>).

The first five identified natural frequencies (Figure 4) of the fixed scaled structure were found to correspond to the following mode shapes (listed in order of identification): rotational around the pier axis (1<sup>st</sup>), longitudinal along the deck axis (2<sup>nd</sup>), closely spaced coupled longitudinal and transverse (3<sup>rd</sup> and 4<sup>th</sup>) and bending (5<sup>th</sup>). Based on the field measurements, these laboratory-identified mode shapes matched the sequence of the first five eigenmodes identified for the actual (real scale) M<sub>3</sub> pier cantilever, with the exception of the two coupled modes (i.e., the 3<sup>rd</sup> and the 4<sup>th</sup> mode of the actual structure, which were identified as uncoupled transverse and uncoupled longitudinal, respectively). From column 3 of Table 2, it can also be observed that

the natural frequencies of the steel, fixed scaled structure ranged between 15.87 and 88.99 Hz. This matched very well to the target frequencies of the ideal (i.e., the theoretical, concrete model scaled to 1:100) structure, as they presented a mere 6.74% average deviation (see Table 2 for deviation definition). This qualitative (in terms of mode shapes and order) and quantitative (in terms of natural frequencies) agreement between the equivalent fixed scaled and the idealized scaled structures was deemed satisfactory and hence, the equivalent steel model was considered reliable enough for the envisaged comparative study.

### **Scaled structure embedded in soil**

Having established a level of confidence regarding the equivalence of the scaled structure to the prototype, additional measurements were performed for two alternative soil types of decreasing stiffness, namely for stabilized soil and Hostun sand.

#### ***Stabilized soil***

A soil can be characterized as stabilized when its stiffness has been increased by lime injection. According to the grain size distribution curve presented in Figure 5 (left), the particular soil used consisted of 75% clay, 10% sand and 15% gravel. Its liquid limit (LL) was equal to 42, and more than 50% of the grain passed the #200 sieve. Based on the above information and the ASTM D2487 (2011) guidelines, the soil was characterized as “gravelly lean clay”. The required percentage of added lime was determined to be 4% according to DIN EN 459-1 (2010) standards. Based on a standard Proctor compaction test, the optimal water content was determined to be 24% and the maximum achieved dry density of the mix was equal to  $\rho_s=1.86\text{t/m}^3$ .

The stabilized soil was placed in six layers of 5 cm height each, within a laboratory box of 95 cm diameter and 40 cm height that was fixed on the shaking table (Figure 6a). For each layer, soil and water were initially mixed at the laboratory mixture machine (Figure 6b) before lime was injected (Figure 6c). Next, each layer was placed inside the laboratory box and was

compacted by a laboratory compaction tool until it reached the target 5 cm height (Figure 6d). The final surface of every layer was manually coarsened with the use of a knife to enhance the cohesion with the overlying layer (Figure 6e). Eventually, the scaled structure was fixed (essentially bolted) on a 15 cm diameter circular concrete foundation of class C30/37 Eurocode 8 (compressive strength,  $f_{ck}=30$  MPa) resembling the caisson of the actual structure, which was embedded in the upper three layers of the stabilized soil (Figures 6f and 7). Four sensors were placed inside the box: two measuring the shear wave velocity ( $V_s$ ) and two measuring the compression wave velocity ( $V_p$ ) of the stabilized soil. The  $V_s$  sensors had a 17 cm separation distance and were placed at a 15 cm height, corresponding to the same level where the base of the concrete foundation was placed inside the box. The  $V_p$  sensors were placed 5 cm below the  $V_s$  sensors at 19.5 cm apart. Due to the reaction of lime with the clay, daily measurements were conducted for 28 consecutive days in order to capture the evolution of the stabilized soil stiffness with time. It is noted, however, that in a preliminary work (Faraonis et al., 2014), the measured values of  $V_s$  did not fully match those predicted by the numerically-based SI. Therefore, a detailed investigation was undertaken to re-assess soil properties for the 28-day measurements. More specifically, the  $V_p$  measurements were utilized to back-assess the  $V_s$  based on Equation 2, by assuming a realistic value for the Poisson's ratio of the stabilized soil ( $\nu = 0.35$ ). Based on this investigation, the  $V_p$  measurement of the 14<sup>th</sup> day (345 m/sec) was used for the numerical model as a representative value of the stabilized soil stiffness; hence, leading to a  $V_s$  value of (166 m/sec), through:

$$V_s = \sqrt{\frac{V_p^2 - 2\nu V_p^2}{2(1-\nu)}} \quad (2)$$

The shear modulus,  $G$ , was then determined to be 51 MPa (for  $V_s=166$  m/s and  $\rho_s= 1.86$  t/m<sup>3</sup>), according to:

$$G = V_s^2 \rho \quad (3)$$

### ***Hostun sand***

In the last case study, the stabilized soil was removed from the laboratory box and replaced by Hostun sand (Figure 8). The Hostun sand was dry and loose with a friction angle  $\phi=35^\circ$ , cohesion  $c=0$  kPa and relative density  $Dr(\%) = 50$ . The total height of the Hostun sand in the box was 35.5cm and its dry density was measured as  $\rho_s=1.33$  t/m<sup>3</sup>. The grain size distribution curve of the Hostun sand is presented in Figure 5 (right curve). The scaled structure was also fixed at the circular concrete foundation of 15 cm diameter and height, which was similarly embedded in the upper 15 cm of the sand. The  $G$  of the Hostun sand was determined to equal 4.6 MPa ( $V_p=96$  m/sec,  $\nu=0.20$ ,  $V_s=59$  m/s and  $\rho_s= 1.33$ t/m<sup>3</sup>) based on a procedure similar to the one described for the stabilized soil.

### ***System identification of the equivalent scaled structure embedded in the two examined soils***

In both soil cases studied, the structure was excited at the deck level by hammer impact loads. The dynamic characteristics of the bridge model structure were then identified based on the same method (i.e., covariance-driven stochastic subspace identification) used for the fixed scaled model. Identical accelerometer arrangements were also employed.

The first five natural frequencies and mode shapes identified at the scaled structure that was founded on stabilized soil ranged between 14.88 and 85.04 Hz, and are presented in column 5 of Table 2 and Figure 9a. Compared with those identified for the fixed-base structure, these identified frequencies were reduced by 4-30% depending on the way in which different modes had been affected by soil compliance. More precisely, the natural frequencies of the bending and rotational modes were reduced by 4% and 6%, respectively, while the natural frequencies of the transverse and the two longitudinal modes, which were directly affected by soil flexibility, were reduced by 15% to 30%. On the other hand, the identified damping ratios at the bridge-

foundation-stabilized soil system ranged between 0.37% and 3.27%, confirming an increase compared to the damping ratios identified for the fixed bridge-foundation system (0.12-0.57%), as shown in columns 5 and 3 of Table 2, respectively.

For the case of the Hostun sand, a further decrease of 19-76% was observed in the identified natural frequencies, which were found to vary between 9.60 Hz and 71.85 Hz (Table 2, column 9). A corresponding increase was also observed in the identified damping ratios (1.27-8.59%) compared to the case of the stabilized soil, as seen in column 9 of Table 2. No difference was observed in the sequence of the first five identified modeshapes, illustrated in Figure 10a.

The decreases in the identified natural frequencies and in the amplification of the identified damping ratios are attributed to the gradually decreasing stiffness of the bridge-foundation system (i.e., shifting from fixed to stabilized soil and then to Hostun sand). As anticipated, even for ambient vibrations, soil stiffness played a significant role in the identified dynamic characteristics of the structure, particularly for translational modes related to vibration along the longitudinal and the transverse axes of the bridge. Assuming, for illustration purposes, that the fixed boundary conditions correspond to a rock condition with a shear wave velocity of 800 m/s, Figure 11 illustrates the above experimentally-verified influence of decreasing soil stiffness on the identified natural frequencies of the scaled bridge structure.

### **Numerical modeling**

In order to investigate the efficiency of existing numerical methods and analytical expressions in simulating the soil stiffness, alternative FE models were developed for the three scaled soil-foundation-pier systems (namely, fixed, stabilized soil and Hostun sand).

#### ***Fixed pier base***

Initially, a refined FE model was developed using three-dimensional (3D) solid elements to simulate the fixed scaled structure (Table 1, column 4). The FE model consisted of approximately 19,000 triangular brick elements with 88,620 DOF. The measured mass of the

physical model was 20.46 kg with a density of  $\rho=7.46 \text{ t/m}^3$ , while the modulus of elasticity of the stainless steel was 210 GPa.

The efficiency of the fixed numerical model in predicting the mode shapes of the constructed fixed scaled structure was assessed by the modal assurance criterion (MAC), which compares vectors of the identified mode shapes with those calculated by a numerical model, essentially through the squared correlation between two modal vectors (Allemang & Brown, 1982):

$$|MAC(\phi_i, \phi_j)| = \left| \frac{\phi_i^T \times \phi_j}{\|\phi_i\| \times \|\phi_j\|} \right| \quad (4)$$

where,  $\phi_i$  is the measured vector of the  $i^{\text{th}} = \{1, \dots, n\}$  mode shape and  $\phi_j$  is the calculated vector of the  $j^{\text{th}} = \{1, \dots, n\}$  mode shape. By definition, the index of the MAC ranges between 0 and 1; the closer the MAC value is to unity, the closer the fit between the measured and the numerically-predicted mode shapes.

### ***Compliant pier base***

For the two cases where the scaled structure was fixed on a circular concrete foundation and embedded into stabilized soil or Hostun sand layers, the pier-foundation-subsoil system was modeled using three alternative approaches.

#### ***Direct method model***

The dynamic stiffness of the soil was first simulated in the 3D space using solid finite elements of approximately 180,000 DOF (Table 1, columns 6 and 10). The G of the stabilized soil was 51 MPa (section 4.1) and the Poisson's ratio was assumed to be  $\nu=0.35$ . For the case of the Hostun sand, G was set to 4.6 MPa (section 4.2) and its Poisson's ratio was assumed to be  $\nu=0.20$ . The same superstructure sections were assumed as for the fixed scaled model, with the properties of stainless steel equal to  $E=210 \text{ GPa}$  and  $\nu=0.30$  along with a C30/37 class concrete

material with  $E=32$  GPa and  $\nu=0.30$  for caisson modeling. The mass of the foundation was measured as 7.56 kg corresponding to a density  $\rho=2.71$  t/m<sup>3</sup>.

#### *Intermediate embedded circular foundation model*

A second approach to model the foundation-soil system (Table 1, columns 7 and 11) was based on the formulas proposed for intermediate embedded circular foundations (for a length-to-diameter aspect ratio,  $2 < D/B < 6$ ). In this case, the superstructure and the foundation were simulated in the same manner as in the first direct approach but springs were employed instead of a 3D soil volume. In particular, the subsoil at the tip of the caisson was modeled as a 6-DOF spring, while the lateral stiffness of the surrounding soil was modeled by an additional 6-DOF spring assigned at the middle of the foundation height. Both 6-DOF stiffness matrices were obtained from the long established theory of surface circular foundations on a stratum over a rigid base as suggested by Kausel (1974) and Kausel and Ushijima (1979) and the solution of Varun et al. (2009) for cylindrically shaped intermediate embedded foundations, respectively (Table 3).

The resulting stiffness terms were derived for the stabilized soil ( $G=51$ MPa,  $\nu=0.35$ ) equal to  $\{K_{h,x}, K_{h,y}, K_v, K_{r,x}, K_{r,y}, K_t\} = \{23297 \text{ kN/m}, 23297 \text{ kN/m}, 38796 \text{ kN/m}, 96 \text{ kNm/rad}, 96 \text{ kNm/rad}, 115 \text{ kNm/rad}\}$  for the tip and  $\{37946 \text{ kN/m}, 37496 \text{ kN/m}, 41767 \text{ kN/m}, 622 \text{ kNm/rad}, 622 \text{ kNm/rad}, 615 \text{ kNm/rad}\}$  for the lateral resistance. For the case of the Hostun sand ( $G=4.6$  MPa,  $\nu=0.20$ ), the stiffness terms of the tip and lateral 6-DOF matrices were  $\{1915 \text{ kN/m}, 1919 \text{ kN/m}, 2826 \text{ kN/m}, 7 \text{ kNm/rad}, 7 \text{ kNm/rad}, 10 \text{ kNm/rad}\}$  and  $\{3024 \text{ kN/m}, 3024 \text{ kN/m}, 3480 \text{ kN/m}, 49 \text{ kNm/rad}, 49 \text{ kNm/rad}, 55 \text{ kNm/rad}\}$ , respectively. Notably, these values are small as a result of the small dimensions of the tested model.

#### *Shallow embedded cylindrical foundation model*

In the third approach (Table 1, columns 8 and 12), the superstructure and the foundation were

again simulated in the same manner as in the first approach, but the soil was replaced by a single set of 6-DOF Winkler type springs, which were placed in the middle of the foundation height. Their values were obtained according to the theory of shallow embedded cylindrical foundations (of a length-to-diameter aspect ratio,  $D/B < 2$ ) resting on a homogenous soil stratum over bedrock, as proposed by Elsabee and Morray (1977) and Gazetas et al. (1985) (Table 3). The stiffness terms for the case of the stabilized soil ( $G=51$  MPa,  $\nu=0.35$ ) were derived equal to  $\{K_{h,x}, K_{h,y}, K_v, K_{r,x}, K_{r,y}, K_t\} = \{79503 \text{ kN/m}, 79503 \text{ kN/m}, 80563 \text{ kN/m}, 623 \text{ kNm/rad}, 623 \text{ kNm/rad}, 731 \text{ kNm/rad}\}$  and  $\{6040 \text{ kN/m}, 6040 \text{ kN/m}, 6307 \text{ kN/m}, 43 \text{ kNm/rad}, 43 \text{ kNm/rad}, 65 \text{ kNm/rad}\}$  for the case of the Hostun sand ( $G=4.6$  MPa and  $\nu=0.20$ ).

### **Comparative assessment of the identified and the numerically-predicted natural frequencies of the tested bridge pier-caisson-soil system**

#### ***Fixed pier base***

Following the identification of the natural frequencies of the fixed base and the two compliant bridge pier-caisson-soil systems, the efficiencies of the developed numerical models to capture the measured dynamic characteristics were studied carefully, starting from the simpler, fixed-base support conditions. It was indeed verified that the first five natural frequencies predicted by the fixed FE model ranged between 16.02 and 89.46 Hz, thus being in very good agreement with those of the fixed structure tested in the laboratory, and which showed a minor average error of 2.12% as summarized in column 4 of Table 2. A visual comparison between the identified and the numerically-predicted mode shapes for the case of the fixed structure is also provided in Figure 4, while a more accurate comparison is illustrated through the MAC values in Figure 12. It is shown that the 1<sup>st</sup> (rotational), 2<sup>nd</sup> (1<sup>st</sup> longitudinal) and 5<sup>th</sup> (bending) modes of vibration matched very satisfactorily, with MAC values close to 1. On the other hand, the numerically-predicted 3<sup>rd</sup> (transverse) and 4<sup>th</sup> (2<sup>nd</sup> longitudinal) modes did not match as successfully (i.e., MAC values 0.68 and 0.60, respectively). This fact is mainly attributed to the



low excitation of the identified 3<sup>rd</sup> and 4<sup>th</sup> modes and to the applied fixed boundary conditions that resulted in the close spacing of these modes (i.e., 65.31 and 66.74 Hz) thus hindering their distinction. As shown in Figures 9 and 10, this limitation is raised for the cases of the stabilized soil and the Hostun sand, where the identified 3<sup>rd</sup> and 4<sup>th</sup> modes were not closely spaced and thus they could easily be distinguished.

### ***Compliant pier base***

Next, the efficiency of the three alternative numerical methods described above was compared in order to predict the dynamic characteristics of the soil-compliant system tested in the laboratory. For the case that simulated the stabilized soil with the direct method model (3D FEs, section 5.2.1) as an intermediate embedded foundation (6+6-DOF springs, section 5.2.2), or as a shallow embedded foundation (6-DOF springs, section 5.2.3), very good matching was observed between the identified and the numerically-predicted frequencies. In particular, the average deviation was found in the order of 3-4% for all methods (Table 2, columns 6, 7 and 8). It is interesting to observe that, despite introducing the compliance of the soil, the error between the experimentally- and the numerically-predicted natural frequencies was not substantially increased compared to the negligible 2% average error that was derived for the fixed system. This observation practically implies that the developed finite element models reliably accounted for the compliance of the stabilized soil and successfully predicted the dynamic properties of the bridge-foundation-clay system. This observation also verifies the prediction made regarding the value of  $G$  (51 MPa) and  $\nu$  (0.35). It is noted herein that as the measurement took place during the 14<sup>th</sup> day of stabilization and the exact hydration phase could not be precisely predicted a lower value of 0.2 was also considered, resulting to an increased error (from 3-4% to 3.2-6.4%).

Repeating the comparison for the case of the Hostun sand, higher deviations were naturally observed between the identified and the numerically-predicted frequencies compared to the case

of the stabilized soil. Namely, the direct method model (section 5.2.1) presented a 13% average error in the identification of the system's natural frequencies, the intermediate embedded foundation method (section 5.2.2) presented a 10% error and the shallow embedded foundation method (section 5.2.3) presented a 12% error (Table 2, columns 10, 11 and 12). These deviations were associated with the inherent limitations of the above numerical approaches that precisely simulate the soil stiffness of loose and non-cohesive soils, as well as to the complex contact issues between the particular soils and the caisson.

It is also interesting to notice that for the soils examined, the identified 3<sup>rd</sup> and 4<sup>th</sup> modes of vibration were not closely spaced anymore (46.38 Hz and 56.86 Hz for stabilized soil, 15.99 Hz and 43.25 Hz for Hostun sand); hence, strong correlations (MAC values over 0.90) were observed with the numerical predictions.

### **Conclusions**

This paper presents the case study of an already constructed, long bridge for which ambient measurements were made available during the construction stage. Based on modal identification at the actual scale and on the ad-hoc designed laboratory experiments at a reduced scale, an effort was made (a) to examine the influence of different soil conditions on the extracted modal parameters of a bridge-foundation-soil system and (b) to compare the efficiencies of alternative numerical approaches in predicting this effect. The conclusions drawn can be summarized as follows:

- The influence of soil compliance on the dynamic characteristics of a bridge-foundation-soil system was demonstrated by all investigative means (i.e., ambient vibrations, laboratory measurements and numerical results), thus highlighting the necessity of carefully considering soil compliance in the framework of design, assessment and structural health monitoring of bridges. According to the laboratory measurements of the fixed scaled structure, introduction of compliant soil deposits (i.e., stabilized soil and

Hostun sand), led to a decrease of all natural frequencies (by 4-30% and 19-76%, respectively). Similarly, the damping ratios of the system were increased for the two soils (by 0.37-3.27% and 1.27-8.59%, respectively) compared to the dynamic characteristics identified for the fixed-base structure.

- For stabilized soil conditions, the discrepancies between the identified and the numerically calculated natural frequencies were in the order of 3-4% on average, that is, close to the negligible 2% under fixed boundary conditions. This observation indicates that the developed numerical models predicted reasonably well the dynamic properties of the bridge-foundation-clay system.
- The fact that all three herein examined numerical models captured efficiently the stiffness of the bridge-foundation-clay system irrespective of their level of modeling complexity demonstrates that simpler, Winkler-type models are adequately capable of numerically predicting soil stiffness at low computational cost compared to the fully fledged, 3D direct method model, provided that these models are prepared carefully according to the literature and are based on reliable measurements of the soil properties. On the other hand, it is noted that the above assessment is only valid for low amplitude ambient vibrations for which the comparisons were made. Notably, in the case of stronger enforced vibrations (i.e., seismic loading) both soil material and geometric nonlinearities may significantly affect the (instantaneous) natural frequencies in the time domain and as such, the reliability of the examined numerical methods needs to be re-verified.
- For the case of Hostun sand soil conditions, more distinct deviations of 10% to 13% were observed between the identified and the numerically calculated natural frequencies. This is primarily attributed to the more extensive nonlinear response that sand materials exhibit even at low levels of strain, and perhaps further to contact issues and ratcheting

effects that essentially limit the efficiency of the examined numerical approaches. The above increased numerical error, however, is an indication of equally increased epistemic uncertainty, which should be taken into consideration in the framework of system identification, even at low levels of vibration.

### **Acknowledgments**

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1 **Table 1. Section and material properties of studied structures and the developed FE models.**

Characteristics	Prototype			Fixed scaled structure				Scaled structure on stabilized soil (14th day)				Scaled structure on Hostun sand			
	(1) Actual Structure	(2) Theoretically scaled	(3) Experiment 1	(4) FEM 1	(5) Experiment 2	(6) FEM 2.1	(7) FEM 2.2	(8) FE model 2.3	(9) Experiment 3	(10) FEM 3.1	(11) FEM 3.2	(12) FEM 3.3			
		Not constructed on site or lab													
Scale	1:1	1:100	Pier height & deck length 1:100	Pier height & deck length 1:100	Pier height, deck length & caisson 1:100	Pier height, deck length & caisson 1:100	Pier height, deck length & caisson 1:100	Pier height, deck length 1:100	Pier height & deck length 1:100	Pier height, deck length & caisson 1:100	Pier height, deck length & caisson 1:100	Pier height, deck length 1:100			
Deck															
Pier															
Caisson			-	-				-				-			
Structure	R/C	R/C	Stainless steel	Stainless steel (E=210GPa)	Stainless steel	Stainless steel (E=210GPa)	Stainless steel (E=210GPa)	Stainless steel (E=210GPa)	Stainless steel	Stainless steel (E=210GPa)	Stainless steel (E=210GPa)	Stainless steel (E=210GPa)			
Soil	Rock (EC8 class A)	Rock (EC8 class A)	Fixed	Fixed	Stabilized soil (Vs=166m/sec)	3D solid elements (G=51MPa)	6+6 DOF <sup>a</sup> springs (G=51MPa)	6-DOF <sup>b</sup> springs (G=51MPa)	Hostun sand (Vs=59m/sec)	3D solid elements (G=4,6MPa)	6+6 DOF <sup>a</sup> springs (G=4,6MPa)	6-DOF <sup>b</sup> springs (G=4,6MPa)			
Foundation	R/C caisson	R/C caisson	-	-	R/C caisson (C30/37)	3D solid elements (E=32GPa)	3D solid elements (E=32GPa)	-	R/C caisson (C30/37)	3D solid elements (E=32GPa)	3D solid elements (E=32GPa)	-			

<sup>a</sup> Based on the formulas of Kausel 1974, Kausel and Ushijima 1979 and Varun et al. 2009

<sup>b</sup> Based on the formulas of Elisabeth and Morray 1977 and Gazetas et al. 1985










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**Table 2. Identified and numerically predicted natural frequencies  $f$  and damping ratios  $\zeta$ .**

	Prototype structure		Fixed scaled structure		Scaled structure on stabilized soil (14th day)				Scaled structure on Hostun sand						
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)			
Actual structure		Theoretically Scaled	Experiment 1	FEM 1	Experiment 2	FEM 2.1	FEM 2.2	FEM 2.3	Experiment 3	FEM 3.1	FEM 3.2	FEM 3.3			
		Not constructed on site or lab													
Modes	f(Hz)	f(Hz)	f(Hz)	ζ(%)	f(Hz)	f(Hz)	ζ(%)	f(Hz)	f(Hz)	ζ(%)	f(Hz)	f(Hz)	f(Hz)		
1-Rotational	0.159	15.90	15.87	0.12	16.02	14.88	0.37	15.18	15.18	15.12	9.60	5.66	11.27	11.31	11.28
2-1 <sup>st</sup> Longit.	0.305	30.50	23.19	0.10	23.13	19.16	0.85	20.16	20.33	19.54	10.49	5.98	10.81	10.94	9.08
3-Transverse	0.623	62.30	65.31	0.57	68.23	46.38	1.56	47.07	47.43	41.88	15.99	8.59	18.18	18.24	14.10
4-2 <sup>nd</sup> Longit.	0.686	68.60	66.74	0.13	69.71	56.86	3.27	58.50	58.28	54.71	43.25	1.94	41.84	41.97	40.35
5-Bending	0.908	90.80	88.99	0.55	89.46	85.04	1.81	87.36	87.60	87.59	71.85	1.27	53.50	64.32	64.31
Average (%) error <sup>a</sup>			6.74% <sup>b</sup>		2.12% <sup>c</sup>			2.86% <sup>d</sup>	3.18% <sup>e</sup>	4.02% <sup>f</sup>			12.61% <sup>g</sup>	9.93% <sup>h</sup>	11.94% <sup>i</sup>

$$^a \left( \sum_{i=1}^5 \left| \frac{f_{1,i} - f_{2,i}}{f_{1,i}} \right| \right) / 5 \times 100$$
, where  $i^{\text{th}} = \{1, \dots, 5\}$  the number of mode

<sup>b</sup>  $f_1$ =Theoretically scaled ,  $f_2$ = Experiment 1

<sup>c</sup>  $f_1$ =Experiment 1,  $f_2$ = FEM 1

<sup>d</sup>  $f_1$ =Experiment 2,  $f_2$ = FEM 2.1, <sup>e</sup>  $f_1$ =Experiment 2,  $f_2$ = FEM 2.2, <sup>f</sup>  $f_1$ =Experiment 2,  $f_2$ = FEM 2.3

<sup>g</sup>  $f_1$ =Experiment 3,  $f_2$ = FEM 3.1, <sup>h</sup>  $f_1$ =Experiment 3,  $f_2$ = FEM 3.2, <sup>i</sup>  $f_1$ =Experiment 23  $f_2$ = FEM 3.3

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15 **Table 3.** Spring coefficients formulas for the herein developed numerical models (6-DOF model & 12-DOF  
16 model.).

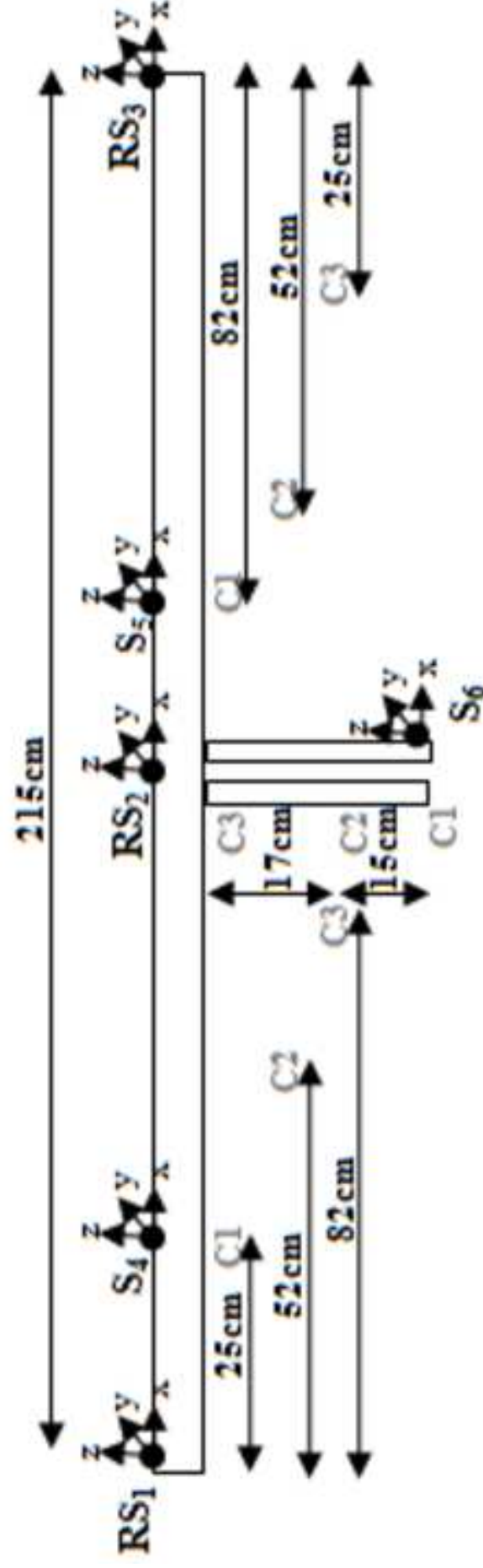
<b>6-DOF model for shallow embedded circular foundation</b>	
<b>6 base springs</b> (Elsabee and Morray 1977 and Gazetas et al. 1985)	
$K_{h,x} = K_{h,y} = \frac{8GR}{2-\nu} \left( 1 + \frac{1}{2} \frac{R}{H} \right)$ (5)	$K_v = \frac{4GR}{1-\nu} \left( 1 + 1.28 \frac{R}{H} \right)$ (6)
$K_{r,x} = K_{r,y} = \frac{8GR^3}{3(1-\nu)} \left( 1 + \frac{1}{6} \frac{R}{H} \right)$ (7)	
$K_t = \frac{16}{3} GR^3$ (8)	
<b>12-DOF model for intermediate embedded circular foundation</b>	
<b>6 base springs</b> (Kausel 1979, Kausel and Ushijima 1979)	
$K_{h,x} = K_{h,y} = \frac{8GR}{2-\nu} \left( 1 + \frac{1}{2} \frac{R}{H} \right) \left( 1 + \frac{2}{3} \frac{D}{R} \right) \left( 1 + \frac{5}{4} \frac{D}{H} \right)$ (9)	
$K_v = \frac{4GR}{1-\nu} \left( 1 + 1.28 \frac{R}{H} \right) \left( 1 + \frac{1}{2} \frac{D}{R} \right) \left( 1 + 0.85 - 0.28 \frac{D}{R} \frac{D/H}{1-D/H} \right)$ (10)	
$K_{r,x} = K_{r,y} = \frac{8GR^3}{3(1-\nu)} \left( 1 + \frac{1}{6} \frac{R}{H} \right) \left( 1 + 2 \frac{D}{R} \right) \left( 1 + 0.7 \frac{D}{H} \right)$ (11)	$K_t = \frac{16}{3} GR^3 \left( 1 + 2.67 \frac{D}{R} \right)$ (12)
<b>springs middle of foundation height</b> (Varun et al. 2009)	
$K_{h,x} = K_{h,y} = 1.828 \left( \frac{D}{B} \right)^{-0.15} ED$ (13)	$K_v = Eq.(10) - Eq.(6)$ (14)
$K_{r,x} = K_{r,y} = (1.06 + 0.227 \frac{D}{B}) ED^2 D$ (15)	$K_t = Eq(12) - Eq.(8)$ (16)

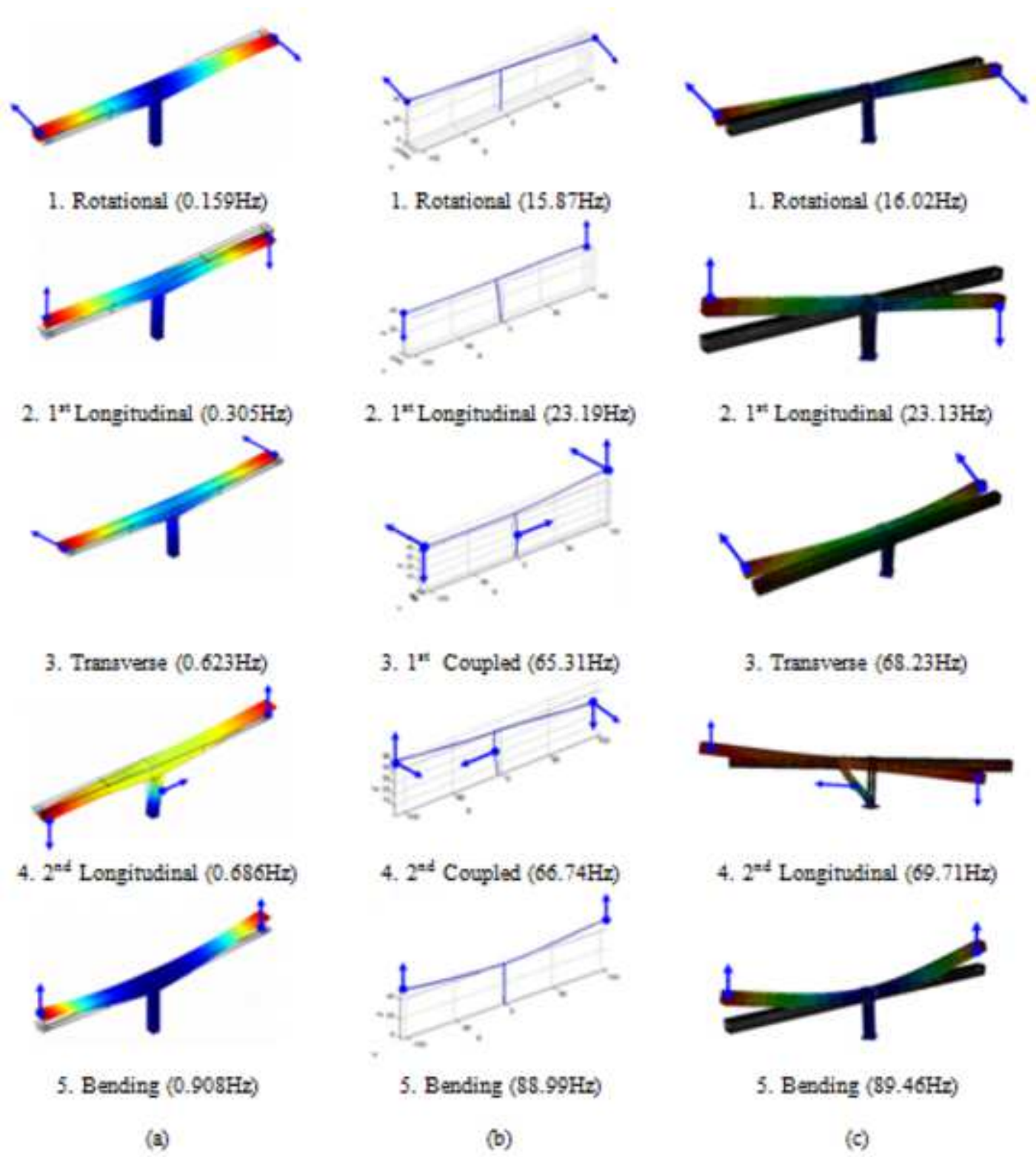
G=shear modulus, E=Young's modulus of Elasticity,  $\nu$ =Poisson's ratio, R=foundation radius, H=height of soil stratum, D=foundation height, B=foundation diameter

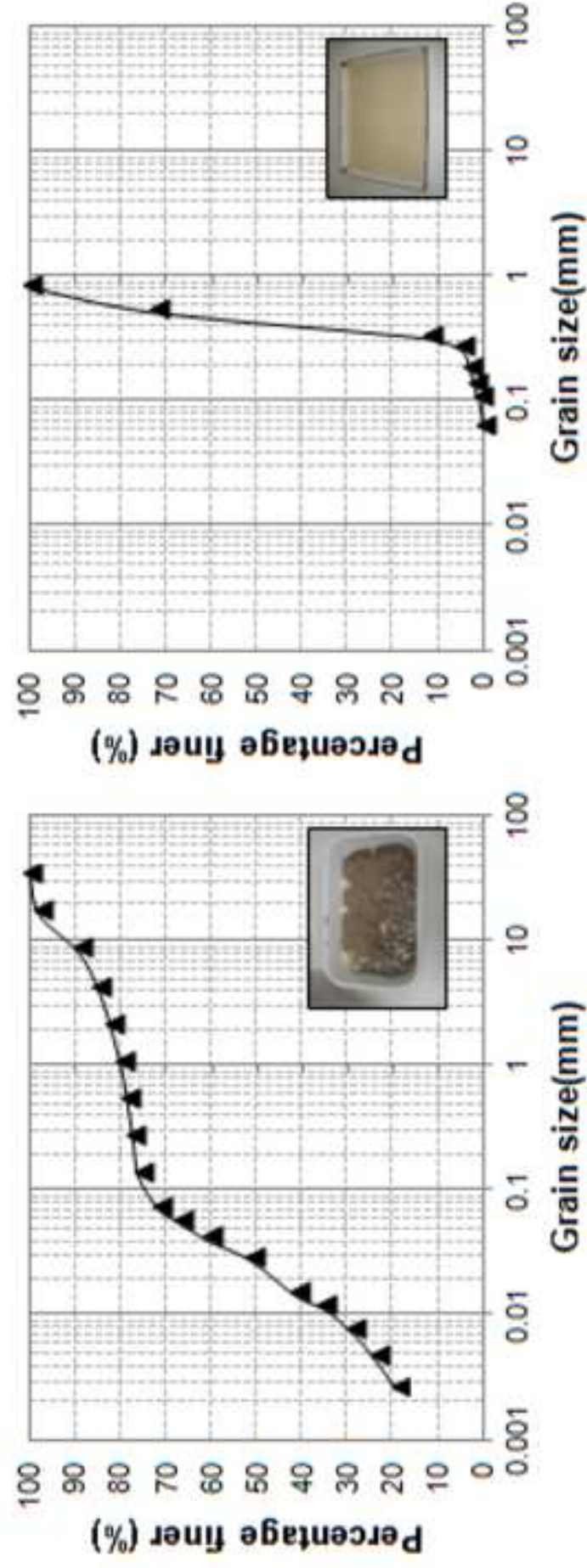
















(a)



(b)



(c)



(d)

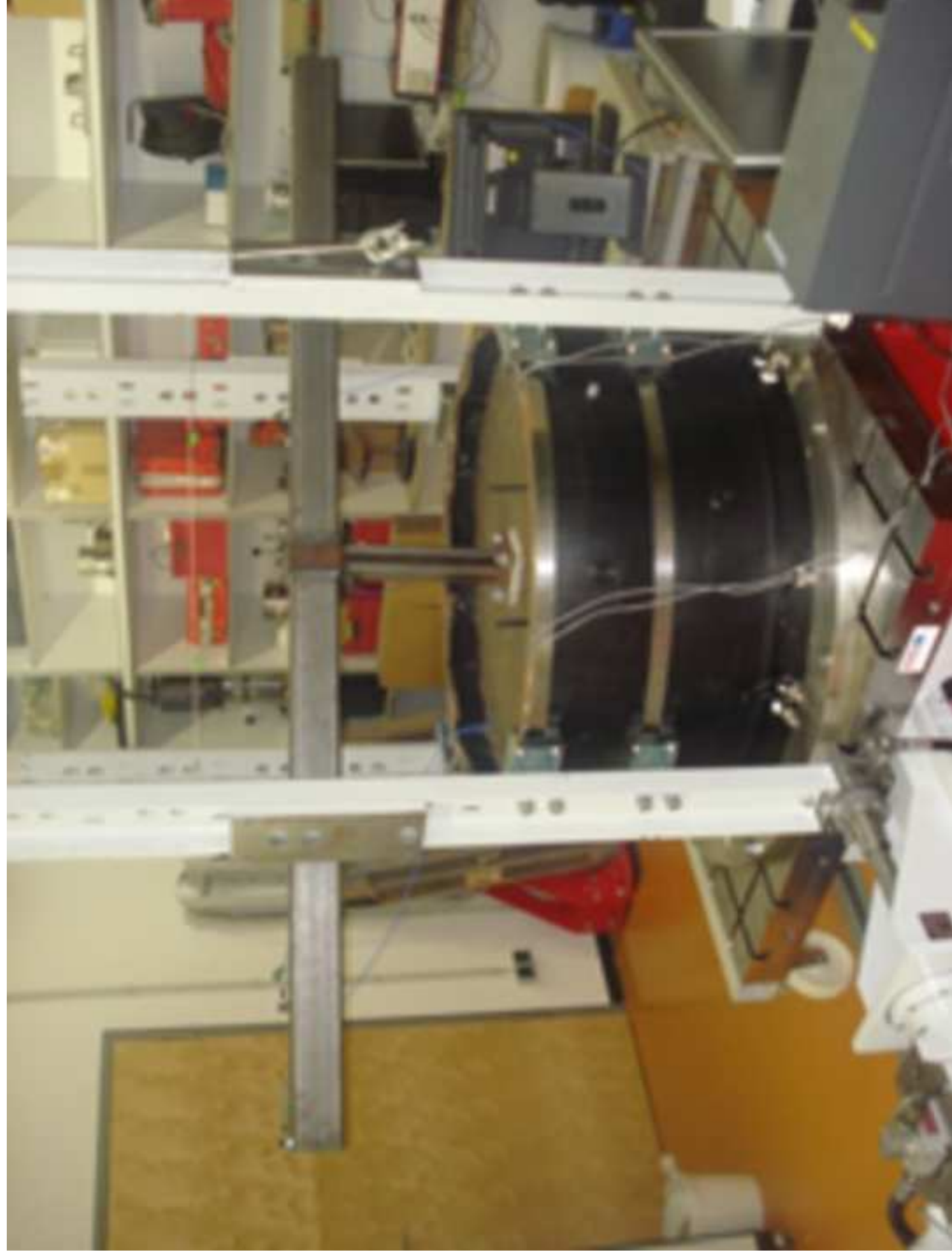


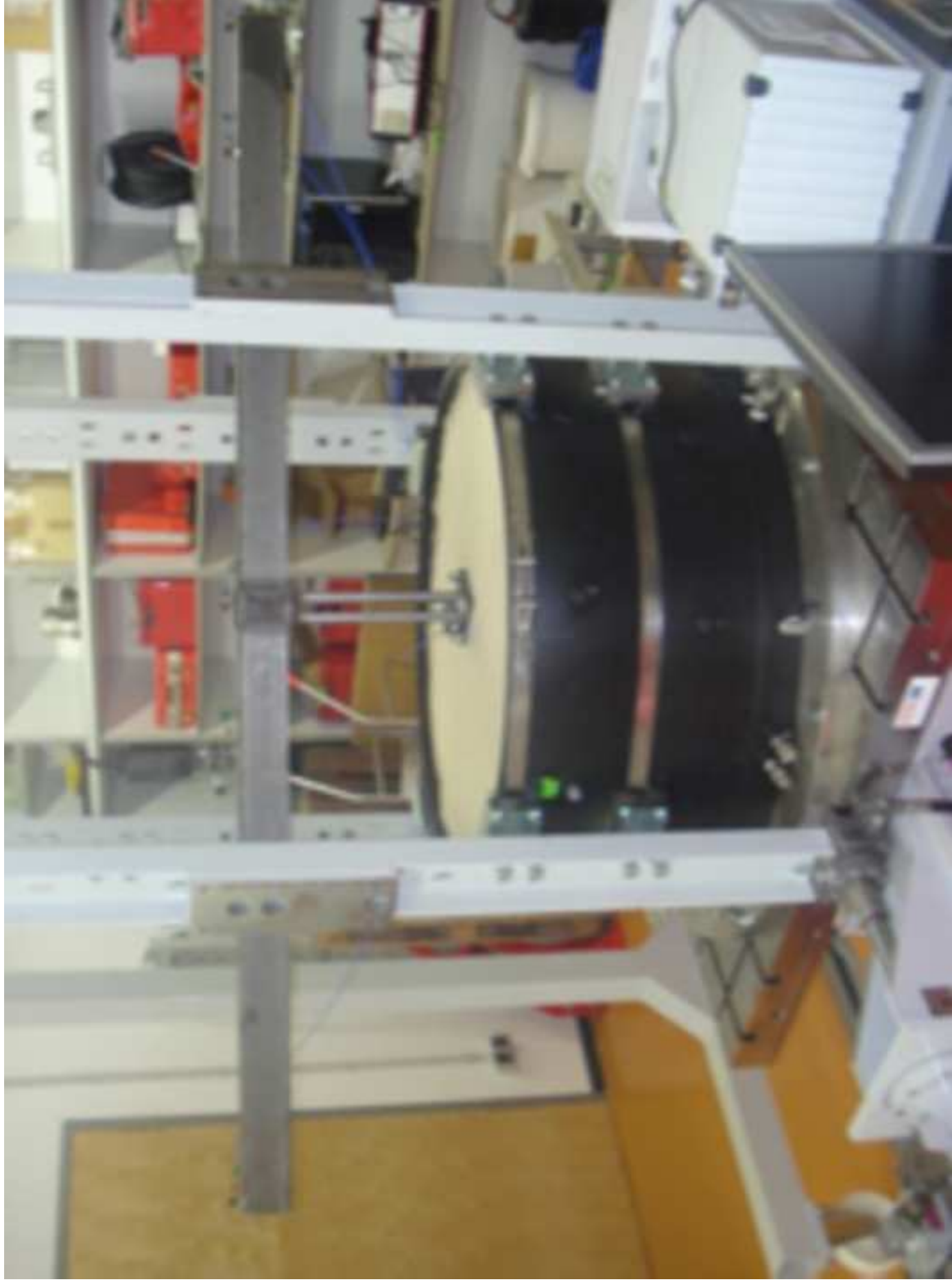
(e)

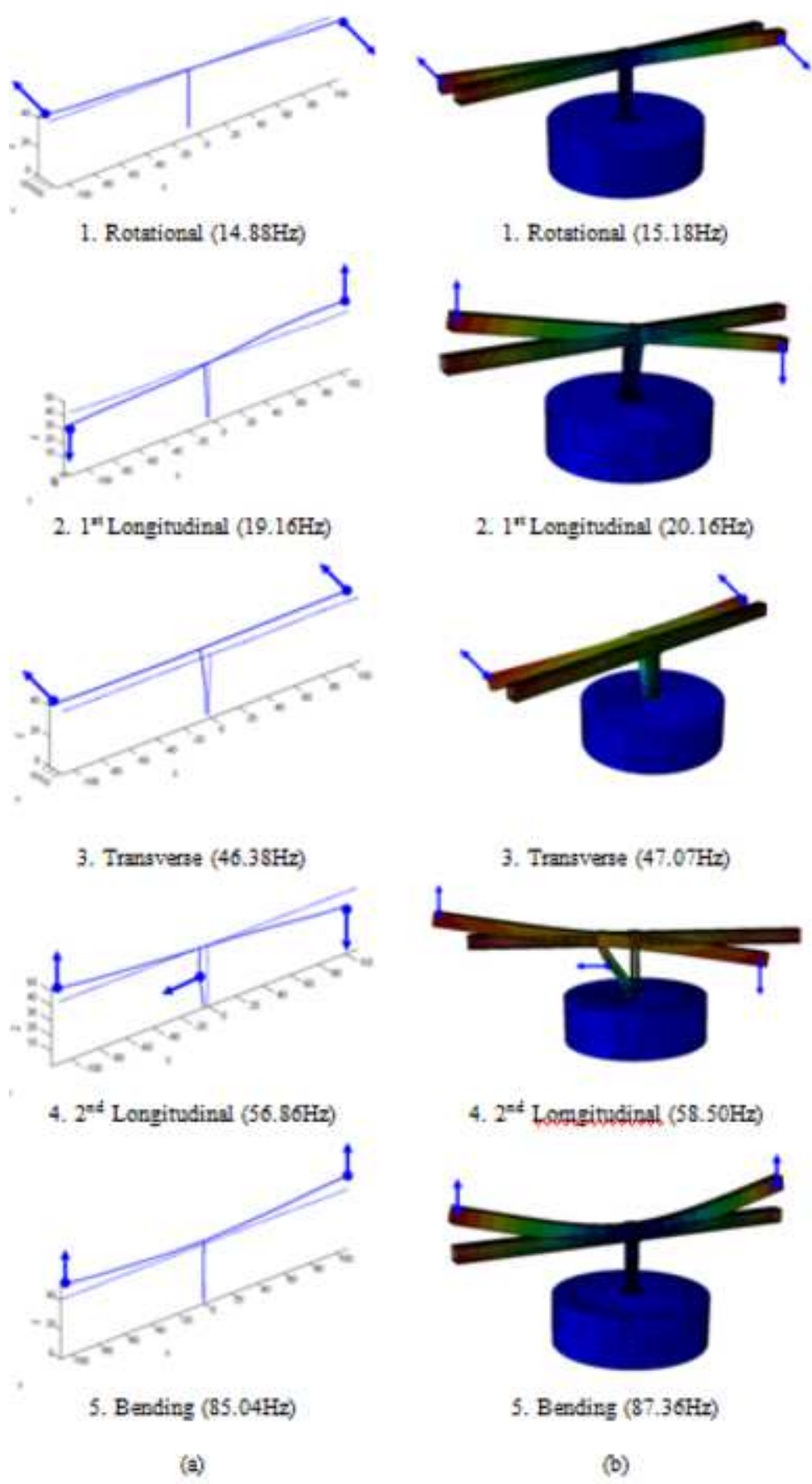


(f)

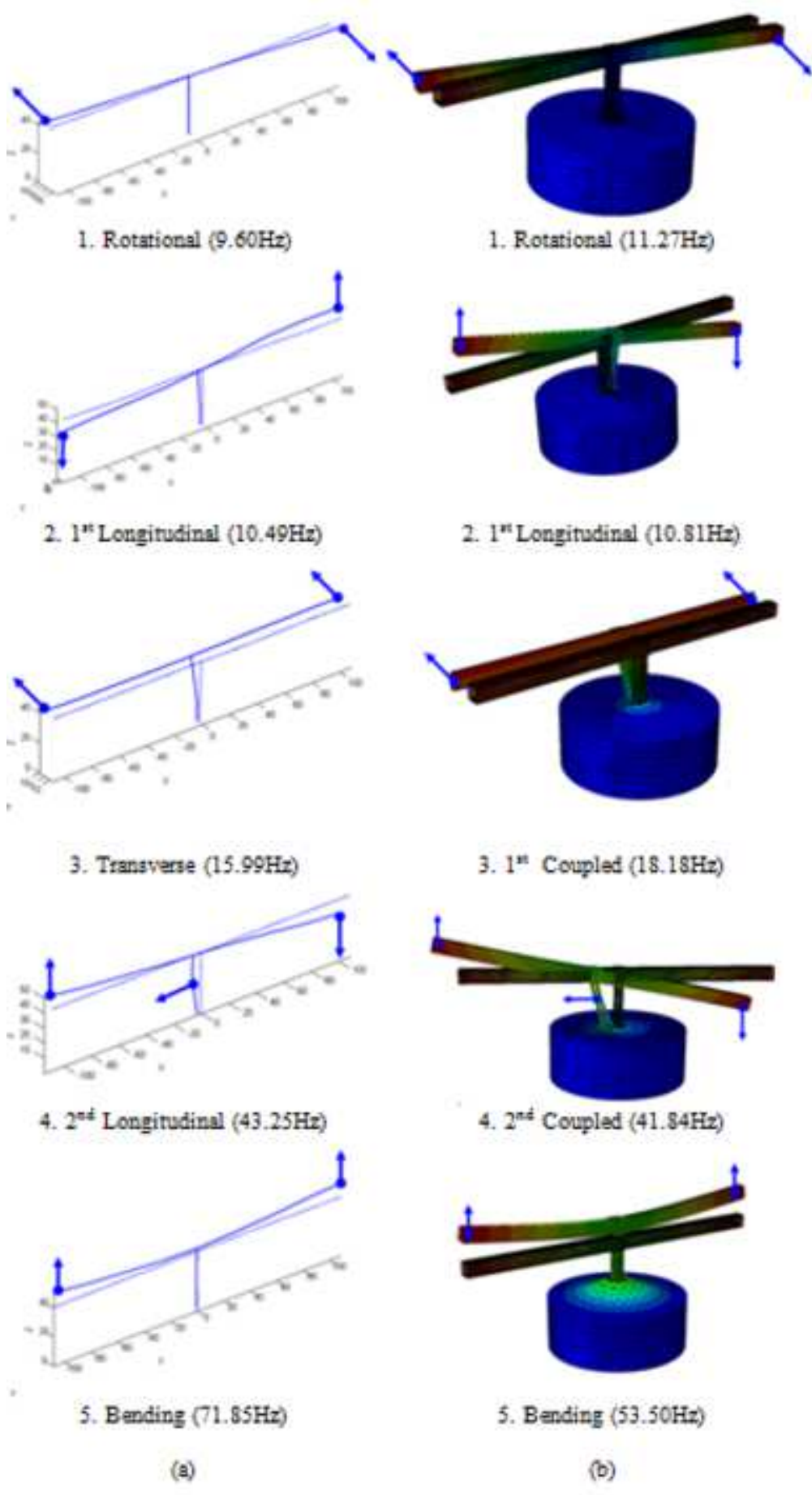
Figure

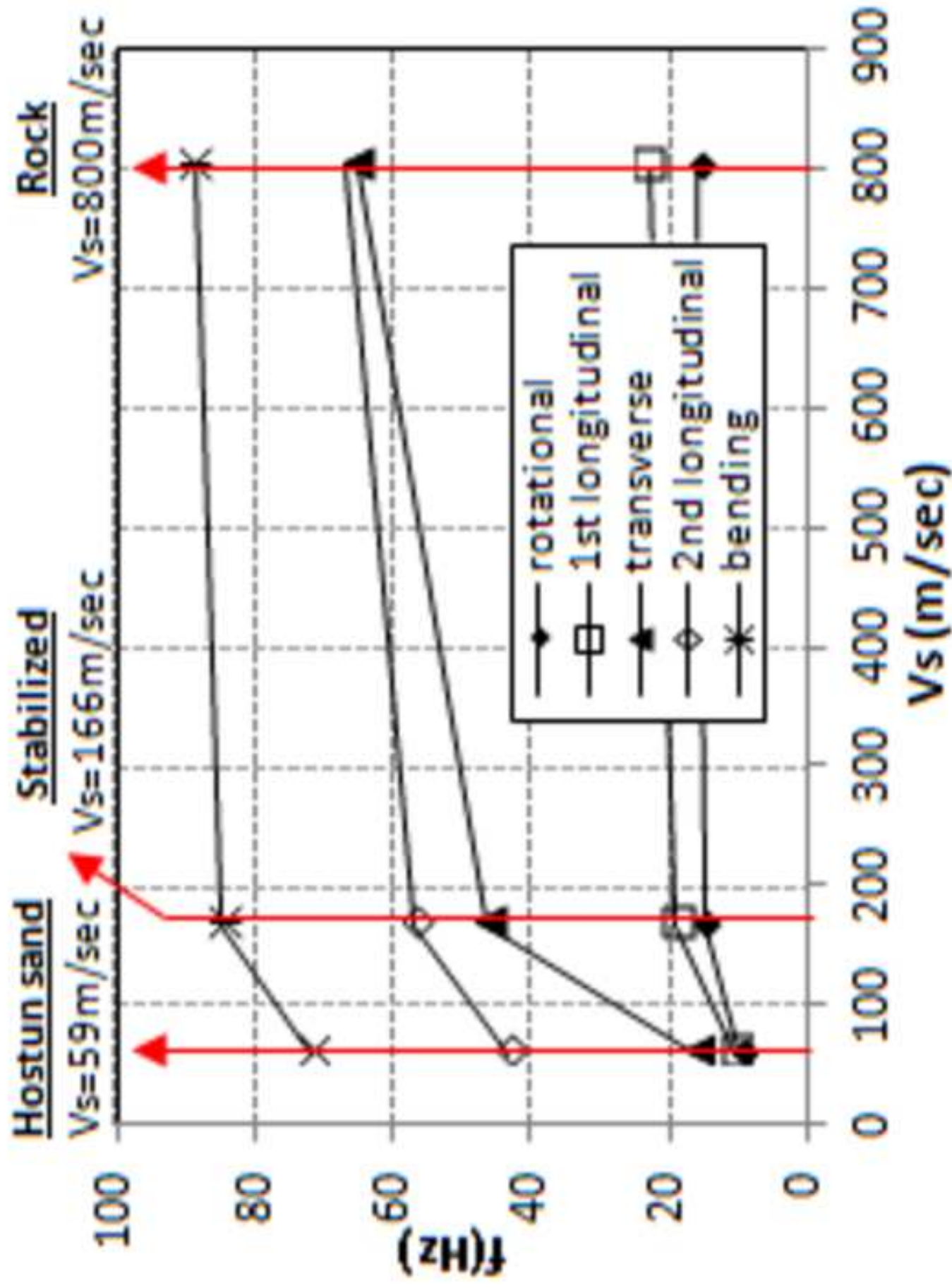


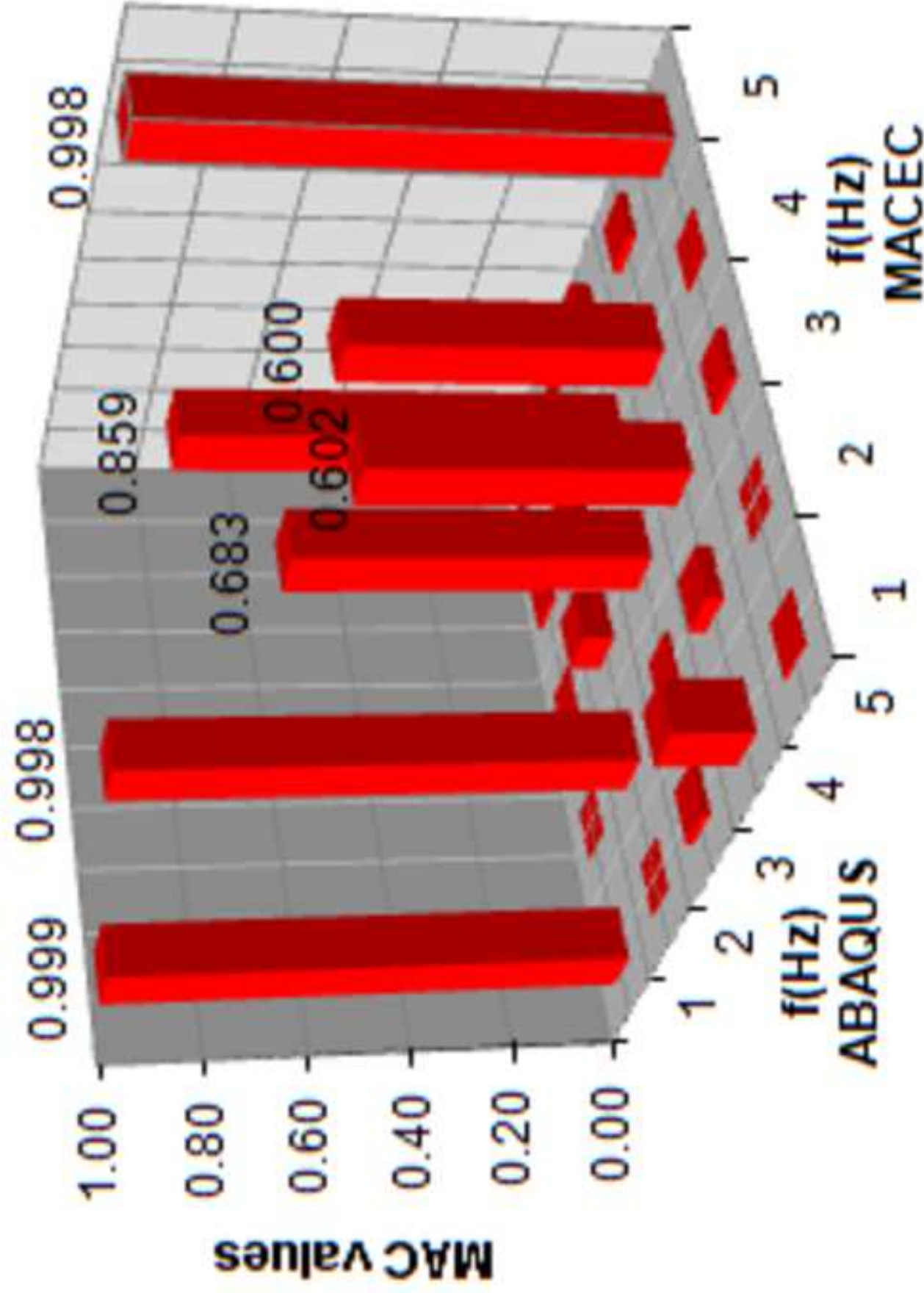












- 1     **Fig. 1.** Metsovo Bridge segments during the construction stage.
- 2     **Fig. 2.** Fixed scaled structure equivalent of Metsovo Bridge M3 pier-deck tested at the laboratory.
- 3     **Fig. 3.** First arrangement (set up 1) of accelerometers and alternative positions of sensors  $S_4$ ,  $S_5$  and  $S_6$   
4     for the two alternative arrangements (set up 2 and set up 3).
- 5     **Fig. 4.** (a) Numerical mode shapes of the full scale model (Panetsos et al 2009, identified  
6     mode shapes of the full scale model also available in Panetsos et al 2009), (b) identified mode  
7     shapes of the fixed scaled model and (c) numerically predicted mode shapes of the fixed  
8     scaled model.
- 9     **Fig. 5.** Grain size distribution curve for the stabilized soil (left curve, before stabilization) and the  
10    Hostun sand (right curve).
- 11    **Fig. 6.** Construction stages of stabilized soil:(a) laboratory box fixed on the shaking table before soil  
12    placement, (b) mixture of the 1<sup>st</sup> soil layer with water at a mixture apparatus, (c) injection of lime to  
13    the mix of soil with water, (d) placement of the 1<sup>st</sup> layer of stabilized soil inside the laboratory box  
14    and compaction until it reached 5cm height, (e) formation of a rough surface with the use of a knife to  
15    enhance cohesion between the 1<sup>st</sup> and the 2<sup>nd</sup> soil layer and (f) embedment of the 15cm concrete  
16    foundation in the last 3 layers of the overall 30cm high (6 layers of 5cm) stabilized soil.
- 17    **Fig. 7.** Scaled structure on stabilized soil.
- 18    **Fig. 8.** Scaled structure on Hostun sand.
- 19    **Fig. 9.** (a) Identified and (b) numerically predicted mode shapes of the scaled structure on stabilized  
20    soil.
- 21    **Fig. 10.** (a) Identified and (b) numerically predicted mode shapes of the scaled structure on  
22    the Hostun sand.



23 **Fig. 11.** Influence of Hostun sand ( $V_s=59\text{m/s}$ ), stabilized soil ( $V_s=166\text{m/s}$ ) and rock ( $V_s=800\text{m/s}$ ) on  
24 the identified modes of the equivalent superstructure of the Metsovo  $M_3$  cantilever.

25 **Fig. 12.** Calculated values of the Modal Assurance Criterion (MAC) between the identified (MACEC)  
26 and numerically predicted (ABAQUS) mode shapes, for the case of fixed boundary conditions.

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Estimating Length of Text		
Count # of words in 3 lines of text:		37
Divided by 3		3
Average # of words per line		12
Count # of text lines per page		24
# of words per page		296.00
Count # of pages (don't add references & abstract)		17.4
Title & Abstract		500
Total # refs	35	848
Length of Text is		6498
		498
		6996
		6

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B. Use ruler and measure figure to fit 1 or 2 column wide format.

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D. Total Characters wide by Total Text lines = word equiv. as shown in the table above. Add word equivalents for each table in the column labeled "Word Equivalents."

Estimating Length of Tables & Figures		
Tables	Word Equivalents	Figures
Table 1	630	Figure 1
2	630	2
3	315	3
4	0	4
5	0	5
6	0	6
7	0	7
8	0	8
9	0	9
10	0	10
11	0	11
12	0	12
13	0	13
14	0	14
15	0	15
Please double-up tables/figures if additional space is needed (ex. 20+21).		16
		17
		18
		19
		20 and 21

Total Tables/Figures:	5201
Total Words of Text:	6996

(word equivalents)

Total words and word equivalents:	12197
printed pages:	10

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subtotal  
plus headings  
TOTAL words  
printed pages

Figures:
Word Equivalents
158
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315
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December 11<sup>th</sup>, 2015

To the Associate Editor of the  
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**Re.:** “Soil-bridge system stiffness identification through field and laboratory measurements” by  
A. Sextos, P. Faraonis, V. Zabel, F. Wuttke, T. Arndt & P. Panetsos

We would like to thank all Reviewers for accepting our manuscript and the Associate Editor for his willingness to check few additional clarifications requested by the XX Reviewer (herein addressed in lines 103-108).

Can we once again thank the Associate Editor for handling the Review process in an excellent manner.

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A handwritten signature in blue ink, appearing to be "AS", followed by a long horizontal stroke.

Dr Anastasios Sextos, MASCE, Associate Professor

On behalf of the co-authors